Understanding XRF Spectrometry

A practical guide
with worked
examples

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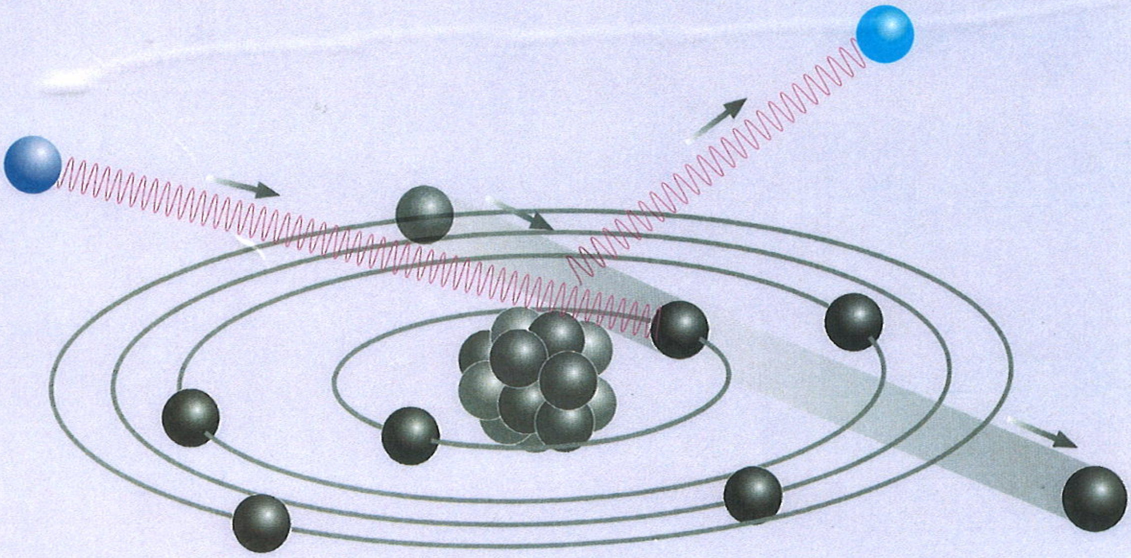

Volume 2

Quantitative
analysis and special
sample preparation
and presentation
methods

Table of Contents

Foreword F-1

F.1 INTRODUCTION F-2
F.2 ACKNOWLEDGEMENTS F-3
F.3 BIBLIOGRAPHY F-4
F.4 SYMBOLS AND TERMINOLOGY F-4
  F.4.1 Symbols F-6
  F.4.2 Influence Coefficients F-6
    F.4.2.1 In the Rousseau algorithm F-6
    F.4.2.2 In the Lachance-Traill algorithm ....

Chapter 13: Introduction to Quantitative Analysis (1) - Choice of Counting Positions and Determination of Background Intensity 13-1

13.1 BASIC TERMINOLOGY 13-1
13.2 CHOICE OF INSTRUMENTAL PARAMETERS AND ANGULAR POSITIONS 13-1
  13.2.1 Selection of X-ray Tube Anode 13-1
  13.2.2 Selection of Analysing Crystal 13-2
  13.2.3 Selection of Detectors 13-2
  13.2.4 Selection of Analyte Lines 13-4
  13.2.5 Infinite Thickness 13-4
  13.2.6 Ba Case Study 13-7
  13.2.7 Selection of Peak and Background Counting Positions 13-9
13.3 CALCULATION OF BACKGROUND INTENSITY BENEATH A PEAK 13-9
  13.3.1 Introduction 13-11
  13.3.2 Method (A) 13-11
  13.3.3 Method (B) 13-12
  13.3.4 Method (C) 13-12
  13.3.5 Method (D) 13-12
  13.3.6 Method (E) 13-13
  13.3.7 Method (F) 13-13
  13.3.8 Method (G) 13-15
  13.3.9 Method (H) 13-16
  13.3.10 Method (I) 13-16
13.4 REFERENCES ....

Chapter 14: Introduction to Quantitative Analysis (2) - Correction Procedures for Spectral Interference and Crystal Fluorescence 14-1

14.1 CORRECTION PROCEDURES FOR SPECTRAL INTERFERENCE (1) 14-1
  14.1.1 Interference from elements present in the sample 14-3
  14.1.2 Example 1 – analysis of Rb, Sr and Y 14-9
  14.1.3 Example 2 – analysis of Ce and Nd 14-13
14.2 CORRECTION PROCEDURES FOR SPECTRAL INTERFERENCE (2) 14-13
  14.2.1 Interference from elements present in the X-ray tube 14-13
  14.2.2 Removal of interfering tube peaks 14-14
  14.2.3 Correction using intensity ratio to a tube line 14-15
  14.2.4 Correction using MACs 14-15
  14.2.5 Example 3 – correction for tube-peak interference (method 1) 14-18
  14.2.6 Example 4 – correction for tube-peak interference (method 2) 14-21
14.3 CORRECTION PROCEDURES FOR CRYSTAL FLUORESCENCE 14-23
14.4 REFERENCES ....

Chapter 15: Introduction to Quantitative Analysis (3) - Methods of Trace Element Standardisation, Determination of Counting Error and Lower Limit of Detection

15.1 INTRODUCTION.....15-1
15.2 METHOD OF STANDARD ADDITION.....15-2
  15.2.1 Technique.....15-2
  15.2.2 Notes.....15-2
15.3 METHOD OF STANDARD DILUTION.....15-3
  15.3.1 Technique.....15-3
  15.3.2 Notes.....15-3
15.4 USE OF AN INTERNAL STANDARD.....15-3
  15.4.1 Technique.....15-3
  15.4.2 Notes.....15-4
15.5 EXTERNAL COMPARISON STANDARDS.....15-6
  15.5.1 Without correction for matrix effects.....15-6
  15.5.2 With correction for matrix effects.....15-7
    15.5.2.1 Regression of Y on X.....15-8
    15.5.2.2 Reduced Major Axis (RMA) Regression.....15-8
    15.5.2.3 Constrained regression through the origin.....15-8
    15.5.2.4 Single point calibration.....15-9
    15.5.2.5. Weighted regression.....15-9
  15.5.3 Advantages of using constrained regression.....15-10
  15.5.4 Using regression.....15-11
15.6 COUNTING ERROR AND LOWER LIMIT OF DETECTION.....15-11
15.7 EXAMPLE – CALCULATION OF CONCENTRATIONS, ERRORS AND LLDs.....15-13
15.8 REFERENCES.....15-17

Chapter 16: Standards and Standard Reference Materials

16.1 INTRODUCTION.....16-1
16.2 LIFE OF STANDARD MATERIALS.....16-1
16.3 IN-HOUSE STANDARDS.....16-2
  16.3.1 Natural standards.....16-2
  16.3.2 Artificial solid standards.....16-2
  16.3.3 Artificial liquid standards.....16-2
16.4 STORAGE OF SRMs.....16-2
16.5 WHERE DO YOU OBTAIN SRMs?.....16-3
16.6 FINDING INFORMATION FOR ANALYTE CONCENTRATIONS.....16-4
16.7 HOW ARE RECOMMENDED VALUES DETERMINED?.....16-5
  16.7.1 Statistical Methods.....16-5
  16.7.2 Abbey's "Select Laboratories" method.....16-7
16.8 DIFFERENT TYPES OF DATA VALUES.....16-7
16.9 PROFICIENCY TESTING.....16-8
16.10 REFERENCES.....16-9

Chapter 17: Introduction to Influence Coefficients

17.1 INTRODUCTION.....17-1
  17.1.1 Basic equations for concentration vs intensity.....17-2
  17.1.2 What are influence coefficients and correction terms?.....17-2
  17.1.3 Factors to be considered in influence coefficient equations.....17-4
    17.1.3.1 Excitation.....17-4
    17.1.3.2 Absorption.....17-4
  17.1.4 Some simple concentration vs intensity equations.....17-5
  17.1.5 Some influence coefficient equations.....17-6
    17.1.5.1 Lachance-Traill (L-T) algorithm.....17-6

17.1.5.2 Claisse-Quintin (C-Q) algorithm 17-7
17.1.5.3 COLA (Comprehensive Lachance) algorithm 17-7
17.1.5.4 Rousseau (RR) algorithm 17-7
17.1.6 Summary 17-7
17.1.7 Link between measured and calculated theoretical "emitted intensities" 17-10
17.2 PRIMARY FLUORESCENCE EMISSIONS DUE TO ABSORPTION 17-13
17.2.1 The concept of absorption correction coefficients 17-17
17.2.2 Derivation of a'_s and a''_s 17-17
17.2.3 Calculating theoretical intensities, measured intensities and concentrations using MACs 17-19
17.3 THE CONCEPT OF ABSORPTION INFLUENCE COEFFICIENTS: a_{ij} 17-20
17.3.1 Derivation of expressions for $a_{ij\lambda}$ 17-21
17.3.2 Detailed derivation of absorption influence coefficient, $a_{ij\lambda}$ 17-22
17.3.3 Calculation of μ_s*, $I_{i\lambda}$, $a_{ij\lambda}$, C_i, $I_{(i)\lambda}$ and g_i (numerical example) 17-24
17.3.4 Transformations of equations (17.11b) and (17.3) 17-24
17.4 THE CONCEPT OF ENHANCEMENT INFLUENCE COEFFICIENTS: $e_{ij\lambda}$ 17-25
17.4.1 Derivation of expressions for $e_{ij\lambda}$ 17-25
17.4.1.1 Detailed derivation of enhancement influence coefficient, $e_{ij\lambda}$ 17-26
17.4.1.2 Multi-element context 17-27
17.4.2 Use and derivation of $e*$ to correct for enhancement 17-29
17.5 SUMMARY 17-34
17.6 REFERENCES 17-34
17.7 APPENDICES 17-35
17.7.1 Appendix 17A: Numerical example of the calculation of μ^*_s, $I_{Ni\lambda}$, $a_{NiFe\lambda}$, C_{Ni}, $I_{(Ni)\lambda}$ and g_{Ni} 17-35
17.7.2 Appendix 17B: A numerical example of the calculation of the enhancement influence coefficient $e_{FeNi\lambda}$ and its application in calculating $I_{i\lambda}$ 17-37
17.7.3 Table 17B-1. Data for computing $a_{FeNi\lambda}$, $e_{FeNi\lambda}$ and $I_{Fe\lambda}$ 17-38

Chapter 18: Mathematical Matrix Correction Techniques

18.1 INTRODUCTION 18-1
18.2 XRF EMISSIONS AND INFLUENCE COEFFICIENTS FOR POLYCHROMATIC EXCITATION SOURCES 18-1
18.2.1 The process of summing monochromatic entities 18-4
18.2.2 Fundamental parameters method 18-4
18.2.3 Influence coefficient algorithms for polychromatic incident radiation 18-5
18.3 A COMPARISON OF SOME CHARACTERISTICS OF SELECTED INFLUENCE COEFFICIENT ALGORITHMS 18-5
18.3.1 Broll-Tertian (B-T) algorithm 18-6
18.3.2 Rousseau (RR) algorithm 18-6
18.3.3 Lachance-Claisse (L-C) algorithm 18-6
18.4 UNDERSTANDING INFLUENCE COEFFICIENTS 18-7
18.4.1 Introduction 18-7
18.4.2 Summary 18-10
18.5 THE CONCEPT OF α_{ij} IN DIFFERENT INFLUENCE COEFFICIENT ALGORITHMS 18-10
18.5.1 The modified Claisse-Quintin (C-Q+) and COLA Algorithms 18-16
18.5.1.1 Cross-correction coefficients, α_{ijk} 18-16
18.5.2 "Eliminated element" algorithms 18-18
18.6 EMPIRICAL INFLUENCE COEFFICIENTS: r_{ij} 18-21
18.6.1 Empirical Coefficient r_{ij} in the Lachance-Traill Algorithm 18-22
18.6.2 Empirical Coefficient r_{ij} in the Lucas-Tooth and Price Algorithm 18-22
18.6.3 Empirical Coefficients r_{ij} and r_{ik} in the Rasberry-Heinrich Algorithm 18-23
18.7 SOME OF THE MORE FREQUENTLY USED CALIBRATION EQUATIONS AND MATRIX CORRECTION ALGORITHMS 18-23
18.8 THE EMPIRICAL APPROACH 18-25

18.9 ALPHA COEFFICIENT MODELS 18-26
18.10 THE FUNDAMENTAL INFLUENCE COEFFICIENT APPROACH 18-27
  18.10.1 Comments on, and explanation of, data in Table 18.9. 18-31
  18.10.2 The de Jongh and JIS Algorithms (eliminating one component) 18-33
  18.10.3 Models Requiring On-line Fundamental Parameters Software 18-33
    18.10.3.1 Broll-Tertian algorithm 18-33
    18.10.3.2 Rousseau algorithm 18-33
    18.10.3.3 Lachance-Claisse algorithm 18-33
18.11 THE FUNDAMENTAL PARAMETERS ALGORITHM/METHOD 18-33
18.12 COMPARISON OF RESULTS FROM SOME INFLUENCE COEFFICIENT ALGORITHMS . 18-34
18.13 DEFINING COMPREHENSIVE ANALYTICAL CONTEXTS 18-41
  18.13.1 Monitors 18-41
  18.13.2 Condensed numerical example of analytical context data 18-42
  18.13.3 Analytical Strategy 18-43
18.14 INFLUENCE COEFFICIENT MODELS - LIMITATIONS, PITFALLS 18-44
18.15 SOME OF THE COMMONLY USED INFLUENCE COEFFICIENT MODELS 18-44
18.16 TYPES OF INFLUENCE COEFFICIENT MODELS 18-45
  18.16.1 Algorithms using the empirical approach (MRA) 18-46
  18.16.2 The fundamental influence coefficient approach 18-47
  18.16.3 Alpha coefficient models (models requiring off-line fundamental parameters software) 18-47
    18.16.3.1 Claisse-Quintin (C-Q) algorithm 18-48
    18.16.3.2 COLA and Lachance-Traill (L-T) algorithms 18-48
  18.16.4 The de Jongh and JIS algorithms 18-48
    18.16.4.1 de Jongh algorithm (DJ) 18-48
    18.16.4.2 Japanese Industrial Standard algorithm (JIS) 18-49
  18.16.5 Models requiring on-line fundamental parameters software 18-49
    18.16.5.1 Broll-Tertian 18-49
    18.16.5.2 Rousseau model 18-50
    18.16.5.3 COLA algorithm 18-50
18.17 SUMMARY 18-50
18.18 ACKNOWLEDGEMENT 18-52
18.19 REFERENCES 18-52
18.20 APPENDIX. NUMERICAL EXAMPLE OF THE CALCULATION OF INFLUENCE COEFFICIENTS FOR THE C-Q+ AND COLA ALGORITHMS 18-54
  18.20.1 C-Q+ algorithm 18-54
  18.20.2 COLA algorithm 18-55

Chapter 19: Glass Disks by Borate Fusions

19.1 INTRODUCTION 19-1
  19.1.1 Undesirable effects of using powders in XRFS 19-1
  19.1.2 Advantages of using fusion techniques 19-1
19.2 PREPARATION OF GLASS DISKS 19-2
  19.2.1 General procedure 19-2
    19.2.1.1 Typical simplified procedure 19-2
    19.2.1.2 A limitation to borate fusion 19-3
  19.2.2 Fluxes and additives 19-3
    19.2.2.1 Fluxes 19-3
    19.2.2.2 Properties of borate fluxes 19-4
    19.2.2.3 Impurities in fluxes 19-5
    19.2.2.4 Additives 19-5
    19.2.2.5 Releasing agents 19-5
  19.2.3 Preparation before fusion 19-7
    19.2.3.1 Fusion mixture 19-7
    19.2.3.2 Crucibles and moulds 19-10

19.2.4 Heating ... 19-11
19.2.4.1 Heating requirements ... 19-11
19.2.4.2 Heating steps ... 19-13
19.2.4.3 Heating steps for oxidation ... 19-13
19.2.4.4 Heating steps for fusion and homogenization ... 19-13
19.2.4.5 Heating steps for conditioning before casting ... 19-15
19.2.5 Casting and cooling ... 19-15
19.2.5.1 Casting into moulds ... 19-15
19.2.5.2 Solidification ... 19-15
19.2.6 Examples of fusions that require special techniques ... 19-18
19.2.6.1 Sulphide minerals ... 19-18
19.2.6.2 Copper compounds ... 19-19
19.2.6.3 Carbon ... 19-19
19.2.6.4 Metallic materials ... 19-20
19.2.6.5 Carbonates ... 19-20
19.3 PYROSULPHATE FUSIONS ... 19-20
19.3.1 Procedure ... 19-20
19.3.2 Automatic preparation ... 19-20
19.3.3 Requirements ... 19-21
19.3.4 Problems ... 19-21
19.3.5 Fusions of sulphide concentrates ... 19-21
19.3.6 Analysis of disks ... 19-21
19.3.7 Conclusions ... 19-22
19.4 FLUXERS ... 19-22
19.4.1 Fusion Instruments ... 19-22
19.5 CARE OF CRUCIBLES AND MOULDS ... 19-22
19.5.1 Crucibles ... 19-22
19.5.2 Moulds ... 19-23
19.6 MISCELLANEOUS ... 19-24
19.6.1 Contamination by crucibles ... 19-24
19.6.2 Blanks ... 19-24
19.6.3 Loss or gain on ignition (LOI or GOI) ... 19-24
19.7 ADVANTAGES AND LIMITATIONS OF FUSION ... 19-25
19.7.1 Advantages ... 19-25
19.7.1.1 Reproducibility ... 19-25
19.7.1.2 Accuracy ... 19-26
19.7.1.3 Preparation of standards ... 19-26
19.7.1.4 Versatility ... 19-26
19.7.1.5 Cost ... 19-26
19.7.2 Limitations ... 19-27
19.7.3 Environment ... 19-27
19.8 SELECTION OF FLUX ... 19-27
19.9 REFERENCES ... 19-28

Chapter 20: Sampling and Specimen Preparation of Geological Materials

20.1 INTRODUCTION ... 20-1
20.2 SAMPLING ERRORS ... 20-3
20.3 STANDARD SIEVE SIZES ... 20-4
20.4 ROCK SPLITTING, CRUSHING AND GRINDING ... 20-5
20.4.1 Grinding aids ... 20-6
20.5 SAMPLE SPLITTING/RIFFLING ... 20-6
20.6 POWDER BRIQUETTE PREPARATION ... 20-8
20.6.1 Binders ... 20-8
20.6.2 Specimen labelling ... 20-8
20.6.3 Briquetting pressure ... 20-8

  20.6.4 Fracturing and pre-pumping of briquettes 20-8
  20.6.5 Particle size effects 20-10
20.7 PREPARATION OF DISKS OF SOLID ROCK 20-11
20.8 FUSIONS 20-13
  20.8.1 Low dilution fusions for trace element analysis 20-13
20.9 SPECIMEN STORAGE 20-13
  20.9.1 Specimen contamination 20-13
20.10 WORN RIMS ON OFTEN-USED POWDER BRIQUETTES 20-14
20.11 REFERENCES 20-16

Chapter 21: Special Sample Preparation Techniques

21.1 INTRODUCTION 21-1
21.2 LIQUIDS 21-1
21.3 VERY SMALL SAMPLES 21-1
21.4 THIN LAYER TECHNIQUES 21-1
  21.4.1 Sample support media 21-4
  21.4.2 Preparation of thin layers from solutions 21-4
  21.4.3 Preparation of thin layers from powders 21-5
  21.4.4 Coprecipitation 21-6
  21.4.5 Use of ion exchangers 21-7
  21.4.6 Preconcentration technique 21-9
21.5 CONTAMINATION 21-10
21.6 ELIMINATING RADIATION FROM THE SAMPLE CUP 21-10
21.7 CONCLUSION 21-11
21.8 REFERENCES 21-12

Chapter 22: Software

22.1 INTRODUCTION 22-1
22.2 NRLXRF 22-1
  22.2.1 Description 22-1
  22.2.2 Source 22-1
22.3 VXRF 22-2
22.4 NBSGSC 22-2
  22.4.1 CALCO 22-3
  22.4.2 CALCOMP 22-3
  22.4.3 Source 22-3
22.5 XRFWIN 22-3
22.6 ROUSSEAU SOFTWARE 22-4
22.7 XRF Direct (CLAISSE ON-LINE MATRIX CORRECTION SOFTWARE) 22-4
  22.7.1 Claisse Calculator for optimal flux composition 22-4
  22.7.2 Claisse website 22-4
22.8 UniQuant® 22-5
  22.8.1 UniQuant® website 22-5
22.9 XrfTable 22-5
22.10 SOME USEFUL WEBSITES 22-6
22.11 REFERENCE 22-7

Summary and Conclusion

S.1 SUMMARY S-1
S.2 ADVANTAGES OF XRFS S-12
S.3 DISADVANTAGES OF XRFS S-13
S.4 CONCLUSION S-15
S.5 REFERENCE S-16

X-ray Tables

T.1 COPYRIGHT PERMISSIONS T-1
T.2 REFERENCES T-1
Periodic Table for XRFS T-3
Table 1. Wavelengths of the principal K X-ray spectral lines (Å) T-4
Table 1a. Wavelengths of the principal K X-ray spectral lines (nm) T-6
Table 2. Wavelengths of the principal L X-ray spectral lines (Å) T-8
Table 2a. Wavelengths of the principal L X-ray spectral lines (nm) T-10
Table 3. Wavelengths of the principal M X-ray spectral lines (Å) T-12
Table 3a. Wavelengths of the principal M X-ray spectral lines (nm) T-14
Table 4. Photon energies of the principal K and L Series X-ray spectral lines T-16
Table 4a. Photon energies of the principal M Series X-ray spectral lines T-18
Table 5. Wavelengths of the K, L and M X-ray Absorption Edges (Å) T-20
Table 5a. Wavelengths of the K, L and M X-ray Absorption Edges (nm) T-22
Table 6. K, L and M X-ray Excitation Potentials and Binding Energies T-24
Table 7-1. Parameters used in Leroux and Thinh equations: $\mu=C.E_{ab}.\lambda^n = C.E_{ab}.(12.3981/E)^n$ $cm^2.g^{-1}$ T-26
Table 7-2. MACs for various wavelengths (λ = 0.31 - 6.0 Å) T-28
Table 7-3. MACs for Kα lines of elements Z = 11 - 60 (Na - Nd) T-31
Table 7-4. MACs for Lα_1 lines of elements Z = 30 - 94 (Zn - Pu) T-36
Table 7-5. MACs for Lβ_1 lines of elements Z = 30 - 94 (Zn - Pu) T-42
Table 8. K and L_{III} Absorption Edge Jump Ratios (r) and (r – 1)/r values T-48
Table 9. Average K, L and M Fluorescence Yields for elements Z = 4-94 .... T-49
Table 10. Relative K and some L Line Intensities within a Series (f_X) T-50
Table 11. Some Useful "Oxide to Element" and "Element to Oxide" conversion factors (gravimetric factors) T-52
Table 12. International Atomic Weights T-53
Table 13. Correspondence between Siegbahn and IUPAC notation for X-ray diagram lines T-54

Index